RISK AND RELIABILITY ANALYSIS

A Handbook for Civil and Environmental Engineers

Vijay P. Singh, Ph.D., P.E. Sharad K. Jain, Ph.D. Aditya Tyagi, Ph.D., P.E.



Risk and Reliability Analysis

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